

## Problem C

# Gray Code

**Input:** standard input

**Output:** standard output

**Time Limit:** 2 seconds

**Memory Limit:** 32 MB

All of you know about Gray Code. It is a number code where consecutive numbers are represented by binary patterns that differ in one bit position only. In the following 4 examples of 3-bit gray code are shown :

```

0 0 0   0 0 0   0 0 0   0 0 0
0 0 1   0 0 1   0 1 0   0 1 0
0 1 1   0 1 1   0 1 1   0 1 1
0 1 0   0 1 0   0 0 1   0 0 1
1 1 0   1 1 0   1 0 1   1 0 1
1 1 1   1 0 0   1 0 0   1 1 1
1 0 1   1 0 1   1 1 0   1 1 0
1 0 0   1 1 1   1 1 1   1 0 0

```

In this problem we will deal with a gray code generation logic. This logic will generate the n-bit gray code using the coding of (n-1) bits. Lets formally define the rules :

- Each gray code has a starting bit pattern. Such as "0 0 0" or "1 0 1" etc.
- An n-bit gray code will have  $2^n$  rows and two consecutive rows will differ by only one bit.
- Each bit pattern will be present exactly once.
- Gray code for 1-bit is trivial. Start with a bit and invert it in the next row.

To construct n-bit gray code keep any of the n bits fixed (either 0 or 1) for the first  $2^{(n-1)}$  rows and use (n-1)-bit gray code (generated using this logic) for remaining (n-1) bits. Then invert the fixed bit for the next  $2^{(n-1)}$  rows and also use (n-1)-bit gray code for remaining (n-1) bits whose bit pattern of the first row is the same as the bit pattern of the last row of previous  $2^{(n-1)}$  rows. For example 2-bit gray code starting with "00" may be :

```

00      00
01      10
11 Or 11
10      01

```

Similarly 2-bit gray code starting with "01" may be :

```

01      01
00      11
10 Or 10
11      00

```

If you observe carefully, you will see that the 3-bit gray codes given above are also constructed using

this logic. Many such gray codes are possible for a particular starting bit pattern. We can order them from 1 to  $G(n)$  where  $G(n)$  denotes the number of such gray codes for  $n$ -bit. In our ordering scheme :

- 1st  $n$ -bit gray code has its leftmost bit fixed and it uses 1st  $(n-1)$ -bit gray code for upper half and also 1st  $(n-1)$ -bit gray code for lower half.
- $G(n-1)$ 'th  $n$ -bit gray code has its leftmost bit fixed and it uses 1st  $(n-1)$ -bit gray code for upper half and  $G(n-1)$ 'th  $(n-1)$ -bit gray code for lower half.
- $[G(n-1)+1]$ 'th  $n$ -bit gray code has its leftmost bit fixed and it uses 2nd  $(n-1)$ -bit gray code for upper half and 1st  $(n-1)$ -bit gray code for lower half.
- $G(n)$ 'th  $n$ -bit gray code has its rightmost bit fixed and it uses  $G(n-1)$ 'th  $(n-1)$ -bit gray code for both halves.

You have to find a  $n$ -bit gray code for given starting bit pattern and index.

## Input

The first line of the input file contains a single integer  $N$  ( $0 < N \leq 1000$ ) which denotes the number of inputs. Each of the next  $N$  lines contains a string of bits for starting bit pattern and an integer for index. Number of bits will be between 1 to 6. And the index will be valid.

## Output

Print the gray code for the given starting bit pattern and index. Put a blank line between two consecutive sets of inputs.

## Sample Input

```
3
000 1
111 5
10 2
```

## Sample Output

```
000
001
011
010
110
111
101
100

111
110
010
011
001
000
100
```

101

10  
00  
01  
11

---

**Author : Md. Kamruzzaman**  
*The Real Programmers' Contest-2*