## Twin Box Pentominoes

Designed by P. F. Ramos 2004, made by Interlocking Puzzles. (wood frame and 12 pieces, $3.75^{\prime \prime} \times 3.75^{\prime \prime} \times 3$ " inches)
Standard pentominoes are the 12 different planar shapes that can be formed from 5 squares. There are 17 non-planar pentomino shapes (each made from 5 cubes). Here, 12 of them (which can be can be grouped into 6 mirror image pairs) must be packed into a $4 \times 5 \times 5$ box frame; 40 units are used by the frame, leaving exactly 60 units of space to pack these pieces:


According to the sheet that came with the puzzle there are 54,189 possible ways these pieces can fit (in the sense that you could build the box around them), of which 23,549 of them can be achieved by starting with the box frame and inserting and moving pieces. Here is the layer by layer representation of the solution that came with the puzzle ( X is the box):

| top layer: | 2nd layer: | 3rd layer: | bottom layer: |
| :---: | :---: | :---: | :---: |
| XXXXX | XGAIX | XGBIX | XXXXX |
| XJAFX | GGAFF | BBBII | XBEIX |
| XJJFX | GJAAK | EEELL | XHELX |
| XCCFX | HJCDK | HHCKK | XHLLX |
| XXXXX | XDDDX | XDCKX | XXXXX |

In the orientations shown in the figures above, pieces can be inserted as follows:

1. B from behind.
2. I from behind.
3. G from behind.
4. H from below.
5. A from behind.
6. F from behind.
7. L from the right.
8. C from above.
9. E from below.
10. K from the front.
11. J from the top.
12. D from the front.
