## Jaap's Puzzle Page

## **Uriblock / Mix Box**



Uriblock, also known as Mix Box, is a type of sliding piece puzzle. It consists of 16 tiles in a 4×4 square. Each row and each column has a slide which can move the 4 tiles in that row or column one square. The top row slide can only move to the right, one square (and then back again), the second row slide only to the left, the third to the right, and the bottom one only to the left. Similarly the columns can only move in alternate directions up and down. Note that this arrangement is symmetric - it looks just the same after a quarter turn of the puzzle. When a slide has been moved, part of the slide has entered the 4×4 area, and so blocks the movement of the nearest perpendicular slide.

The 16 tiles are coloured, four of each of the colours red, yellow, green, and blue. The aim is to arrange them in rows (or equivalently columns).

The puzzle is somewhat similar to the <u>Rubik's Fifteen</u> and <u>Tsukuda's Square</u> (a.k.a 'lt'). Uriblock was invented by and named after Dario Uri. It was made in the mid eighties. It is mentioned in <u>Cubic Circular Issue 7/8</u>, p19.

If your browser supports JavaScript, then you can play Uriblock by clicking the link below:

## JavaScript Uriblock

## The number of positions:

Suppose the slides are in their original positions, so that the tiles form a square. There are 16 tiles, so there are at most 16! positions. This limit is not reached because there are 4 sets of 4 identical tiles. This gives  $16! / 4!^4 = 63,063,000$  positions. However, the 4 colours can be considered identical - it does not matter what order the colours are in the solution. There are therefore only  $16! / 4!^5 = 2,627,625$  positions.

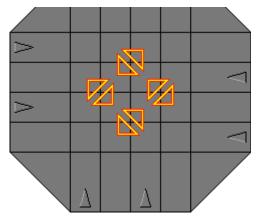
Solution:



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Suppose you slide a row, then a column, then slide the row back, and finally slide the column back. The effect of such a manoeuvre is that three tiles have been swapped around. The affected tiles are the one at the intersection of the column and row, and the adjacent tiles that are moved into that intersection. The picture on the right shows all possible 3-cycles that occur this way. To move the three tiles of a particular triangle in the picture, just alternately move the row and column that lie along the triangle sides.

With the above insight, it becomes quite easy to solve all the pieces of the puzzle except for the corners. To move a corner, slide it in the direction of the clockwise next corner (the only other direction to slide this tile brings it outside the 4×4 area which is pointless). The tile can be moved using the 3-cycle that doesn't involve the slide you just moved.



For example, the top-left corner can be moved to the right, and then with the second row slide and second column slide you can do a 3-cycle. This way you can replace the tile by one of the middle tiles of the second row. Then slide the top row back to the left.

I won't describe a solution in full detail, but the steps below should suffice.

- a. Solve the four corners one by one.
- b. Solve row 1, the top row.
- c. Put the correct tile at row 2, column 1.
- d. Find one of the tiles that could belong in row 2 column 2, and place it at row 3 column 1, without disturbing the previously solved pieces.
- e. Put the correct tile at row 3 column 1. When you do this, the tile at that position gets displaced to row 2 column 2, where it belongs.
- f. Turn the whole puzzle a quarter turn clockwise, and repeat steps c-e.
- g. Now the last 4 tiles, the middle tiles on the bottom two rows.

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