Problem Set 2, Part 1 - Modal Logic

cs112

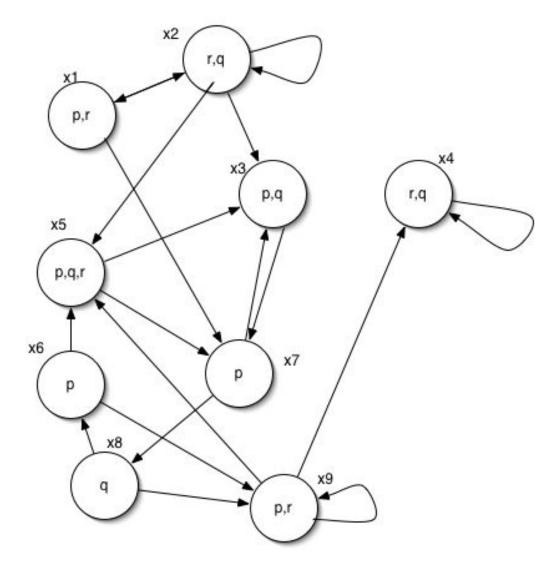
Posted: Tue, September 26, 2006

Due Date: Tue, October 3, 2006 Note: October 3 is a Brandeis Monday. There will be an envelope in the CS office for you to leave your homework.

Exercise 1 Kripke Models

Part 1.1

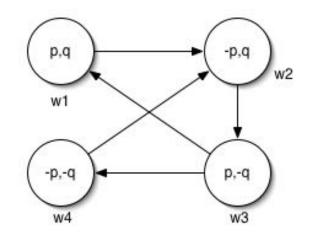
Consider this model:



- 1. Find all worlds satisfying:
 - (a) $x \Vdash \Diamond (p \land q);$
 - (b) $x \Vdash \Box (p \lor r);$
- **2.** Does $x_1 \Vdash \Diamond \Box q$? Show why or why not.
- **3.** Does $x_7 \Vdash \Box \Box \Diamond p$? Show why or why not.
- 4. Does $x_9 \Vdash \Diamond (r \lor \Diamond p)$? Show why or why not.
- 5. Decide whether the following formulas are valid in the model:
 - (a) $\Diamond p \lor \Diamond q$
 - (b) $\Box(r \land \Diamond p)$

Part 1.2

Consider the simple model below:



Decide whether the following formulas are valid in the model:

- **a.** $\Diamond \Box p \lor \Diamond \Diamond \Box p$
- **b.** $\Box p \rightarrow \neg p$
- **c.** $\Diamond (p \lor \neg p) \to \Box (p \lor \neg q)$