## Problem Set 2

## cs112

Posted: Wednesday, October 8, 2008

Due Date: Tuesday, October 28, 2008 IN CLASS

## Exercise 1 Modal Logic

Part 1.1

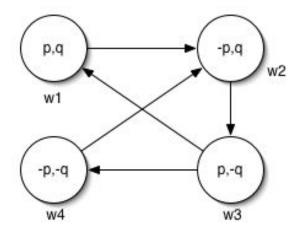
Consider the following model:

x2 r,q p,r p,q r,q x5 p,q,r x6 x7 p x8 x9 p,r

- 1. Find all worlds satisfying:
  - (a)  $x \Vdash \Diamond (p \land q)$ ;
  - **(b)**  $x \Vdash \Box (p \lor r);$
- **2.** Does  $x_1 \Vdash \Diamond \Box q$ ? Show why or why not.
- **3.** Does  $x_7 \Vdash \Box\Box\Diamond p$ ? Show why or why not.
- 4. Does  $x_9 \Vdash \Diamond (r \lor \Diamond p)$ ? Show why or why not.
- 5. Decide whether the following formulas are valid in the model:
  - (a)  $\Diamond p \vee \Diamond q$
  - **(b)**  $\Box(r \land \Diamond p)$

## Part 1.2

Consider the simple model below:



Decide whether the following formulas are valid in the model:

- **a.**  $\Diamond \Box p \lor \Diamond \Diamond \Box p$
- **b.**  $\Box p \rightarrow \neg p$
- **c.**  $\Diamond(p \vee \neg p) \to \Box(p \vee \neg q)$