Scheme in Scheme: The Metacircular Evaluator
Eval and Apply

CS21b: Structure and Interpretation of Computer Programs
Brandeis University
Spring Term, 2016
The *metacircular evaluator* is

A rendition of Scheme, *in Scheme*, where expressions and environments are just *list structures* that get modified according to fixed rules.

A concise language description (as opposed to, say, English) -- which, of course, you need to know Scheme already to understand.

A kind of *fixed point* of the Scheme interpreter.

*factorial* is not a fixed point.

A straightforward medium to discuss language modifications among language designers

No more complicated than many of the programs we have discussed in class

What you are about to learn is powerful, secular wizardry.
Your life will never be the same again.
(define (eval exp env)
  (cond ((self-evaluating? exp) exp)
       ((variable? exp) (lookup-variable-value exp env))
       ((quoted? exp) (text-of-quotiation exp))
       ((assignment? exp) (eval-assignment exp env))
       ((definition? exp) (eval-definition exp env))
       ((if? exp) (eval-if exp env))
       ((lambda? exp)
          (make-procedure (lambda-parameters exp)
                          (lambda-body exp)
                          env))
       ((begin? exp)
          (eval-sequence (begin-actions exp) env))
       ((cond? exp) (eval (cond->if exp) env))
       ((application? exp)
          (apply (eval (operator exp) env)
                 (list-of-values (operands exp) env)))
       (else
          (error "Unknown expression type — EVAL" exp)))))
Apply (coroutines with Eval)

(define (apply procedure arguments)
  (cond ((primitive-procedure? procedure)
             (apply-primitive-procedure procedure arguments))
        ((compound-procedure? procedure)
             (eval-sequence
              (procedure-body procedure)
              (extend-environment
               (procedure-parameters procedure)
               arguments
               (procedure-environment procedure))))
        else
             (error "Unknown procedure type — APPLY" procedure))))

(define (list-of-values exps env)
  (if (no-operands? exps)
      '()
      (cons (eval (first-operand exps) env)
             (list-of-values (rest-operands exps) env))))

(define (apply-primitive-procedure proc args)
  (apply-in-underlying-scheme
   (primitive-implementation proc) args))
Syntax-directed evaluation (examples)

(define (eval-if exp env)
  (if (true? (eval (if-predicate exp) env))
      (eval (if-consequent exp) env)
      (eval (if-alternative exp) env)))

(define (eval-sequence exps env)
  (cond ((last-exp? exps) (eval (first-exp exps) env))
        (else (eval (first-exp exps) env)
              (eval-sequence (rest-expss exps) env)))))

(define (eval-assignment exp env)
  (set-variable-value! (assignment-variable exp)
    (eval (assignment-value exp) env)
    env)
  'ok)

(define (eval-definition exp env)
  (define-variable! (definition-variable exp)
    (eval (definition-value exp) env)
    env)
  'ok)

(define (make-procedure parameters body env)
  (list 'procedure parameters body env))

(define (compound-procedure? p)
  (tagged-list? p 'procedure))
Environments

(define (enclosing-environment env) (cdr env))
(define (first-frame env) (car env))
(define the-empty-environment '())

(define (make-frame variables values)
  (cons variables values))
(define (frame-variables frame) (car frame))
(define (frame-values frame) (cdr frame))

(define (add-binding-to-frame! var val frame)
  (set-car! frame (cons var (car frame)))
  (set-cdr! frame (cons val (cdr frame))))

(define (extend-environment vars vals base-env)
  (if (= (length vars) (length vals))
    (cons (make-frame vars vals) base-env)
    (if (< (length vars) (length vals))
      (error "Too many arguments supplied" vars vals)
      (error "Too few arguments supplied" vars vals))))
Environments (variable lookup)

(define (lookup-variable-value var env)
  (define (env-loop env)
    (define (scan vars vals)
      (cond ((null? vars)
                 (env-loop (enclosing-environment env)))
              ((eq? var (car vars))
               (car vals))
              (else (scan (cdr vars) (cdr vals))))))
  (if (eq? env the-empty-environment)
      (error "Unbound variable" var)
      (let ((frame (first-frame env)))
        (scan (frame-variables frame)
        (frame-values frame))))
  (env-loop env))
Environments (variable lookup)

(define (set-variable-value! var val env)
  (define (env-loop env)
    (define (scan vars vals)
      (cond ((null? vars)
            (env-loop (enclosing-environment env)))
        ((eq? var (car vars))
         (set-car! vals val))
        (else (scan (cdr vars) (cdr vals)))))
    (if (eq? env the-empty-environment)
        (error "Unbound variable — SET!" var)
        (let ((frame (first-frame env)))
          (scan (frame-variables frame)
            (frame-values frame)))))
    (env-loop env))

(define (define-variable! var val env)
  (let ((frame (first-frame env)))
    (define (scan vars vals)
      (cond ((null? vars)
            (add-binding-to-frame! var val frame))
        ((eq? var (car vars))
         (set-car! vals val))
        (else (scan (cdr vars) (cdr vals)))))
    (scan (frame-variables frame)
      (frame-values frame))))
Environments (variable lookup)

(define (setup-environment)
  (let ((initial-env
          (extend-environment
            (primitive-procedure-names)
            (primitive-procedure-objects)
            the-empty-environment)))
    (define-variable! 'true #t initial-env)
    (define-variable! 'false #f initial-env)
    initial-env))
Driver loop

(define input-prompt ";;; M-Eval input:" )
(define output-prompt ";;; M-Eval value:" )

(define (driver-loop)
  (prompt-for-input input-prompt)
  (let ((input (read)))
    (let ((output (eval input the-global-environment)))
      (announce-output output-prompt)
      (user-print output))
  (driver-loop))

(define (prompt-for-input string)
  (newline) (newline) (display string) (newline))

(define (announce-output string)
  (newline) (display string) (newline))

(define (user-print object)
  (if (compound-procedure? object)
      (display (list 'compound-procedure
                      (procedure-parameters object)
                      (procedure-body object)
                      '<procedure-env>))
      (display object)))
;;; M-Eval input:
5
;;; M-Eval value:
5

;;; M-Eval input:
(+ 5 7)
;;; M-Eval value:
12

;;; M-Eval input:
((lambda (x) (* x x)) 5)
;;; M-Eval value:
25

;;; M-Eval input:
(define square (lambda (x) (* x x)))
;;; M-Eval value:
ok

;;; M-Eval input:
(square 5)
;;; M-Eval value:
25

;;; M-Eval input:
(define fact (lambda (n) (if (= n 0) 1 (* n (fact (- n 1)))))
;;; M-Eval value:
ok

;;; M-Eval input:
(fact 5)
;;; M-Eval value:
120

Using the metacircular evaluator...