



# CS114 Lecture 14

## Dependency Grammars and Functional Unification Grammars

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Professor Meteer

Slides from UPenn, Adapted from slides by  
Kathy McCoy, University of Delaware

# Another Earley Example

Spec  $\rightarrow$  S  
S  $\rightarrow$  NP VP  
S  $\rightarrow$  VP  
NP  $\rightarrow$  Det Noun  
NP  $\rightarrow$  PrN  
VP  $\rightarrow$  V  
VP  $\rightarrow$  V NP  
Det  $\rightarrow$  a | the  
N  $\rightarrow$  book  
V  $\rightarrow$  Mark | read  
PrN  $\rightarrow$  Mark

## CHART 1

S0	Spec $\rightarrow$ S		
S1	S $\rightarrow$ . NP VP	[0,0]	Predictor
S2	S $\rightarrow$ . VP	[0,0]	Predictor
S3	NP $\rightarrow$ . Det Noun	[0,0]	Predictor
S4	NP $\rightarrow$ . PrN	[0,0]	Predictor
S5	Det $\rightarrow$ . A	[0,0]	Predictor
S6	Det $\rightarrow$ . the	[0,0]	Predictor
S7	PrN $\rightarrow$ . Mark	[0,0]	Predictor
S8	VP $\rightarrow$ . V	[0,0]	Predictor
S9	VP $\rightarrow$ . V NP	[0,0]	Predictor
S10	V $\rightarrow$ . Mark	[0,0]	Predictor
S11	V $\rightarrow$ . read	[0,0]	Predictor

# Chart 1: Mark read

## CHART 1

S0	Spec → S		S12	PrN → Mark .	[0,1]	Scanner	S7
S1	S → . NP VP	[0,0]	S13	V → Mark .	[0,1]	Scanner	S10
S2	S → . VP	[0,0]	S14	VP → V .	[0,1]	Completer	S13
S3	NP → . Det Noun	[0,0]	S15	S → VP .	[0,1]	Completer	S14
S4	NP → . PrN	[0,0]	S16	Spec → S .	[0,1]	Completer	S15
S5	Det → . A	[0,0]	S17	VP → V . NP	[0,1]	Completer	S13
S6	Det → . the	[0,0]	S18	NP → PrN .	[0,1]	Completer	S12
S7	PrN → . Mark	[0,0]	S19	S → NP . VP	[0,1]	Completer	S18
S8	VP → . V	[0,0]	S20	NP → . Det Noun	[1,1]	Predictor	S17
S9	VP → . V NP	[0,0]	S21	NP → . PrN	[1,1]	Predictor	S17
S10	V → . Mark	[0,0]	S22	Det → . a	[1,1]	Predictor	S20
S11	V → . read	[0,0]	S23	Det → . the	[1,1]	Predictor	S20
			S24	PrN → . Mark	[1,1]	Predictor	S21
			S25	VP → . V	[1,1]	Predictor	S19
			S26	VP → . V NP	[1,1]	Predictor	S19
			S27	V → . Mark	[1,1]	Predictor	S25,26
			S28	V → . read	[1,1]	Predictor	S25,26

# Chart 2: Mark Read

## Chart 2

S29 V → read .	[1,2]Scanner	
S30 VP → V .	[1,2]Completer	S29
S31 VP → V . NP	[1,2]Completer	S29
S32 S → VP .	[1,2]Completer	S30
S33 Spec → S .	[1,2]Completer	S32
S34 S → NP VP .	[0,2]Completer	S19, S30
<b>S35 Spec → S.</b>	<b>[0,2] Completer</b>	<b>S34</b>

<b>S35 Spec → S .</b>	<b>[1,2] Completer</b>	<b>S34</b>
S34 S → NP VP .	[0,2]Completer	S19, S30

S30 VP → V .	[1,2]Completer	S29
S29 V → read .	[1,2]Scanner	

S19 S → NP . VP	[0,1]Completer	S18
S18 NP → PrN .	[0,1]Completer	S12
S12 PrN → Mark .	[0,1]Scanner	S7

# Dependency Grammars

- In CFG-style phrase-structure grammars the main focus is on *constituents*.
- But it turns out you can get a lot done with just binary relations among the words in an utterance.
- In a **dependency grammar** framework, a parse is a tree where
  - the nodes stand for the words in an utterance
  - The links between the words represent dependency relations between pairs of words.
    - Relations may be typed (labeled), or not.

# Well-formedness

- A dependency graph is **well-formed** iff
  - **Single head**: Each word has only one head.
  - **Acyclic**: The graph should be acyclic.
  - **Connected**: The graph should be a single tree with all the words in the sentence.
  - **Projective**: If word A **depends** on word B, then all words between A and B are also **subordinate** to B (i.e. dominated by B).

# Comparison

- Dependency structures explicitly represent
  - Head-dependent relations (**directed arcs**)
  - Functional categories (**arc labels**)
  - Possibly some structural categories (parts-of-speech)
- Phrase structure explicitly represent
  - Phrases (**non-terminal nodes**)
  - Structural categories (**non-terminal labels**)
  - Possibly some functional categories (grammatical functions)

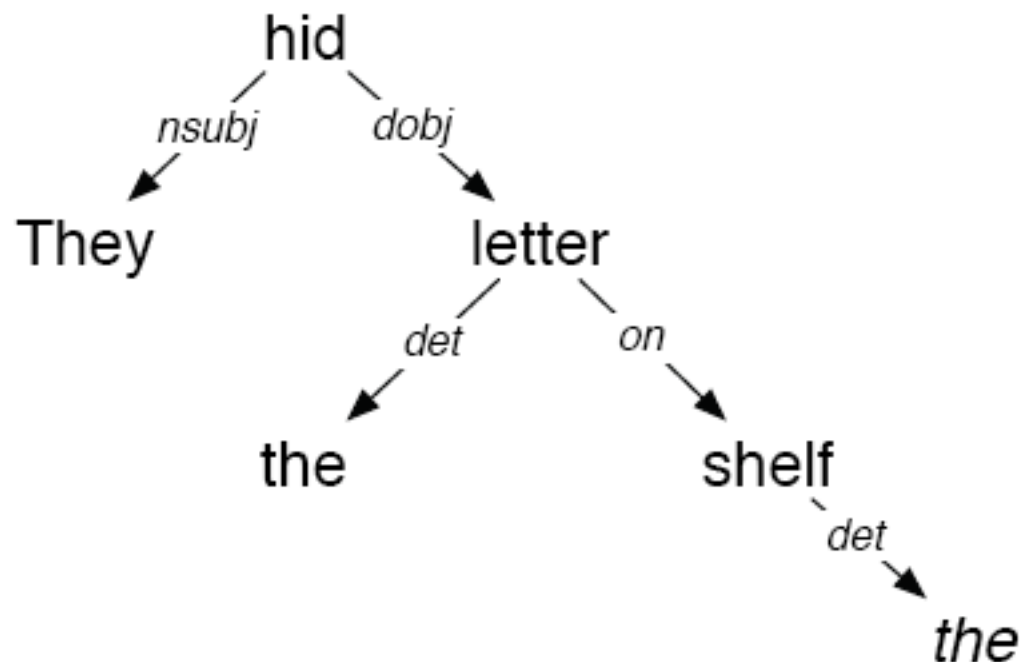




# Dependency Relations

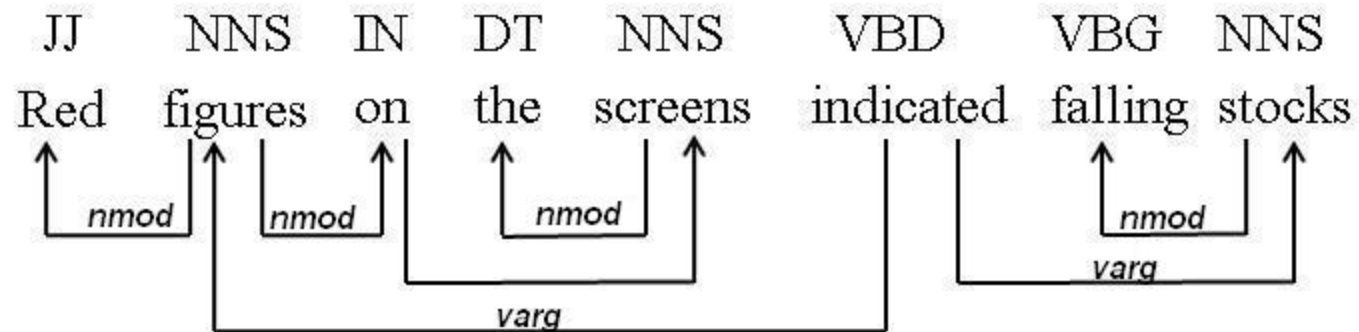
<b>Argument Dependencies</b>	<b>Description</b>
<b>nsubj</b>	nominal subject
<b>csubj</b>	clausal subject
<b>dobj</b>	direct object
<b>iobj</b>	indirect object
<b>pobj</b>	object of preposition
<b>Modifier Dependencies</b>	<b>Description</b>
<b>tmod</b>	temporal modifier
<b>appos</b>	appositional modifier
<b>det</b>	determiner
<b>prep</b>	prepositional modifier

# Dependency Parse



*They hid the letter on the shelf*

# Dependency Tree with Labels



# Dependency Parsing

- The dependency approach has a number of advantages over full phrase-structure parsing.
  - Deals well with free word order languages where the constituent structure is quite fluid
  - Parsing is much faster than CFG-based parsers
  - Dependency structure often captures the syntactic relations needed by later applications
    - CFG-based approaches often extract this same information from trees anyway.

# Dependency Parsing

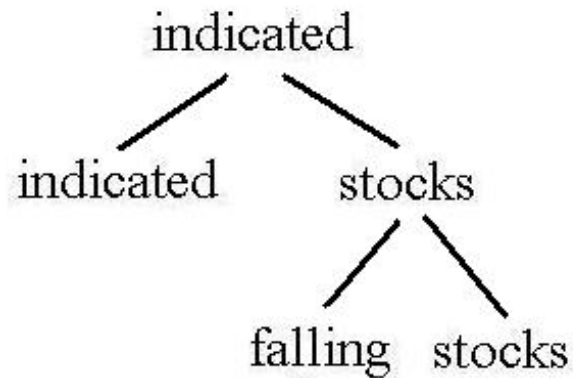
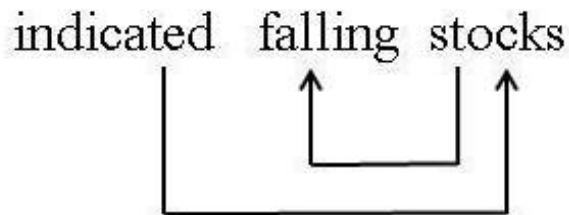
- There are two modern approaches to dependency parsing
  - Optimization-based approaches that search a space of trees for the tree that *best* matches some criteria
  - Shift-reduce approaches that greedily take actions based on the current word and state.

# Parsing Methods

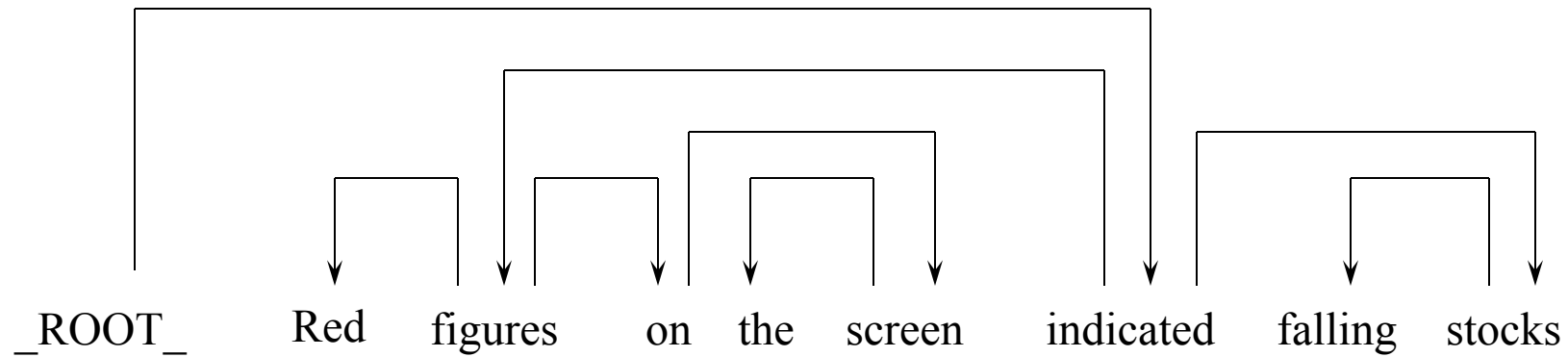
- Three main traditions
  - **Dynamic programming**
    - CYK, Eisner, McDonald
  - Constraint satisfaction
    - Maruyama, Foth et al., Duchier
  - Deterministic search
    - Covington, Yamada and Matsumoto, Nivre

# Dynamic Programming

- Basic Idea: Treat **dependencies** as **constituents**.
- Use, e.g. , CYK parser (with minor modifications)

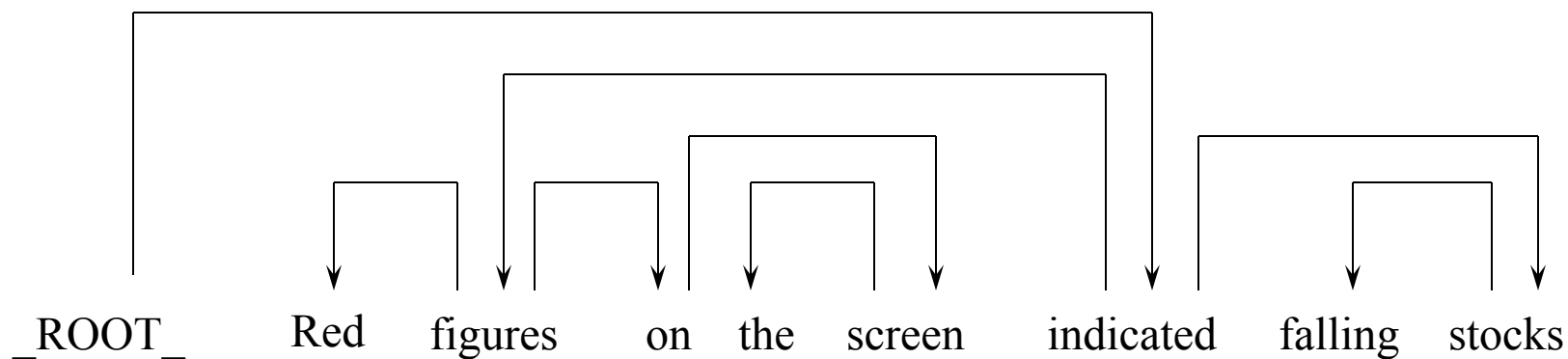


# Example





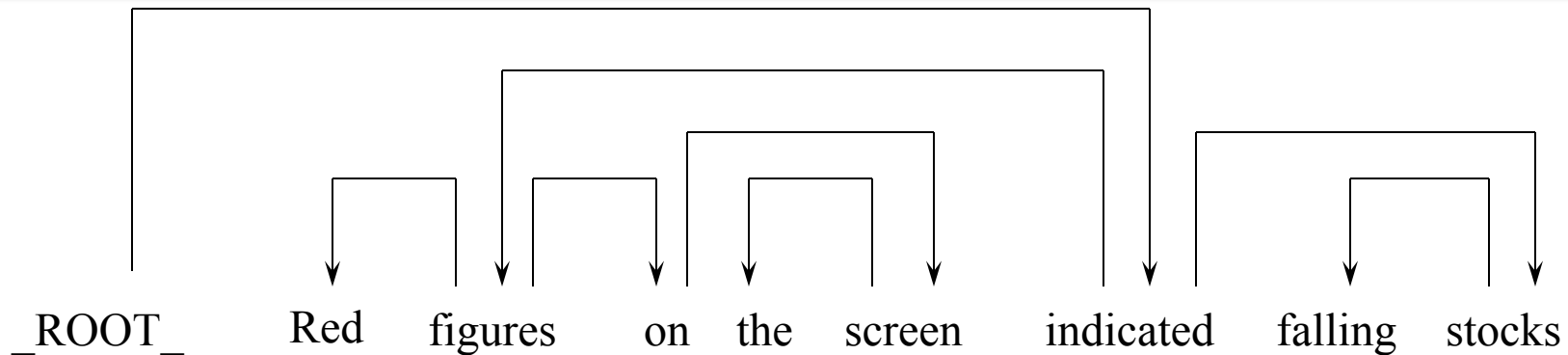
# Example



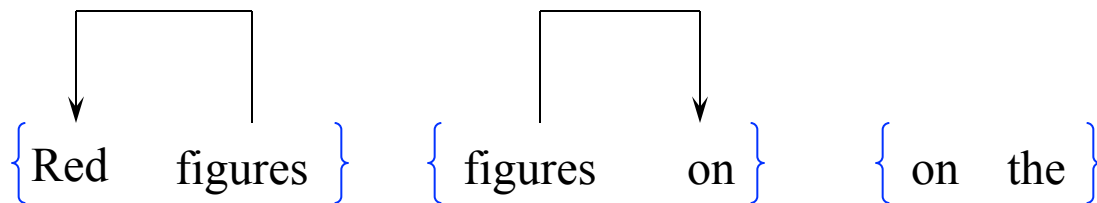
## Spans:



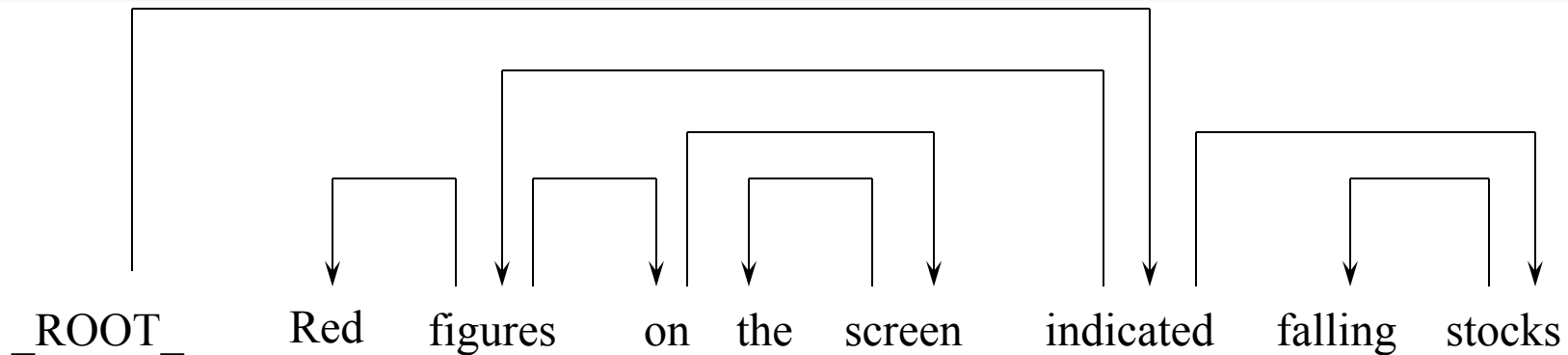
# Assembly of correct parse



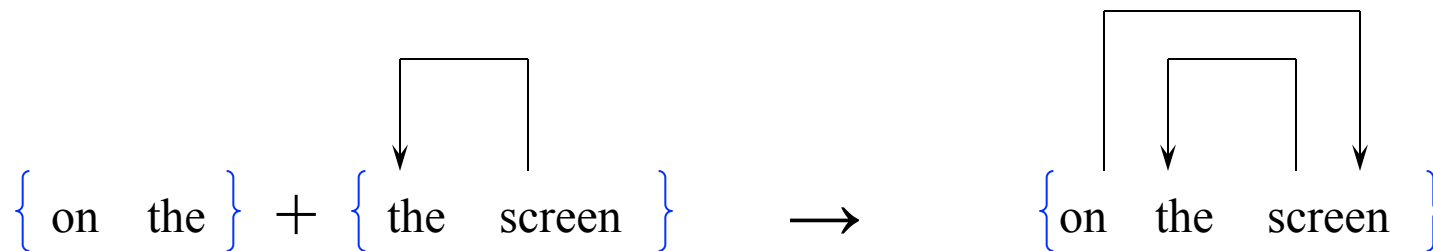
**Start** by combining adjacent words to **minimal** spans



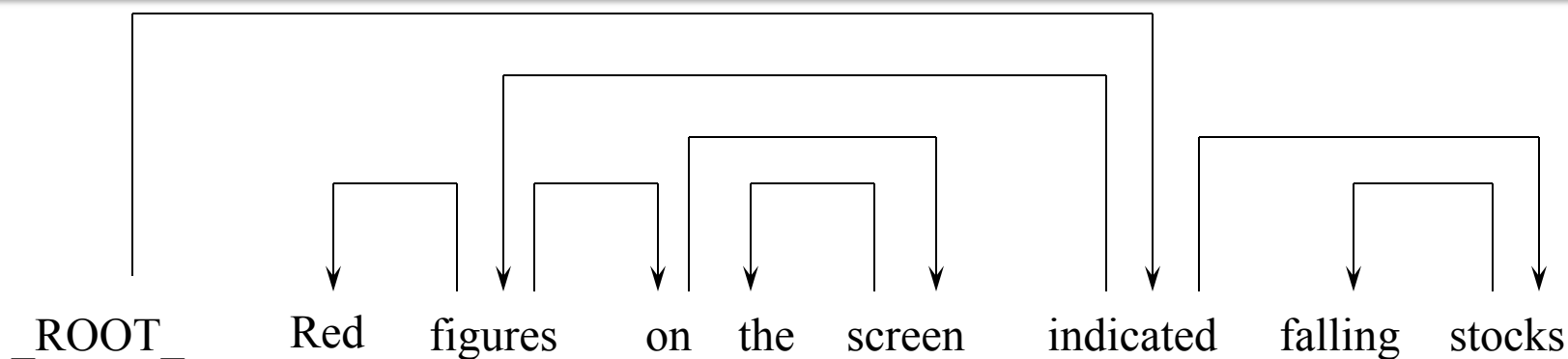
# Assembly of correct parse



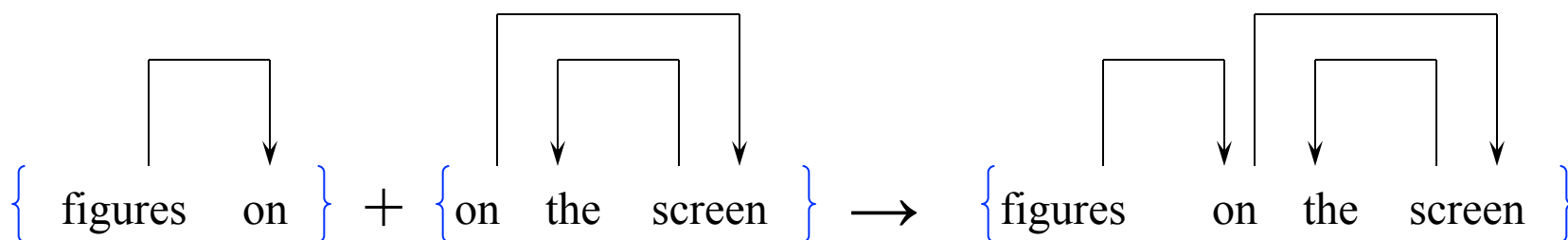
**Combine** spans which overlap in one word; this word must be governed by a word in the left or right span.



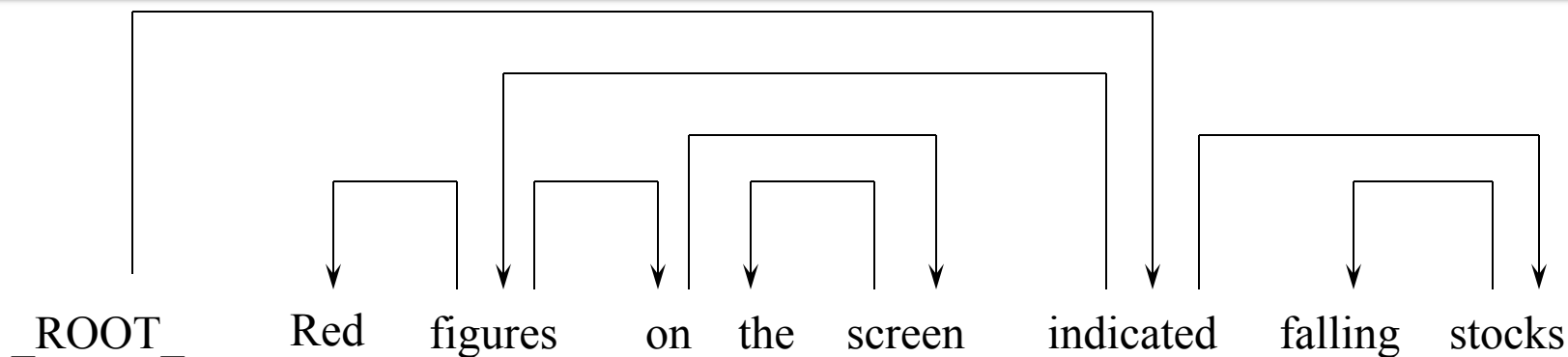
# Assembly of correct parse



**Combine** spans which overlap in one word; this word must be governed by a word in the left or right span.

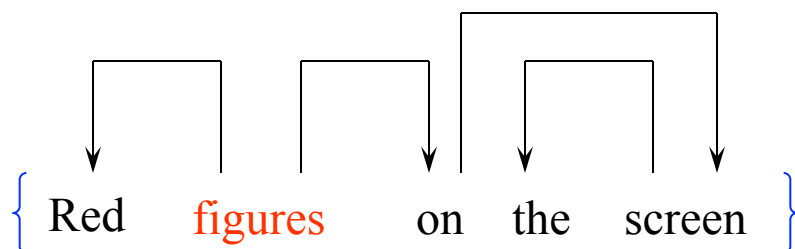


# Assembly of correct parse

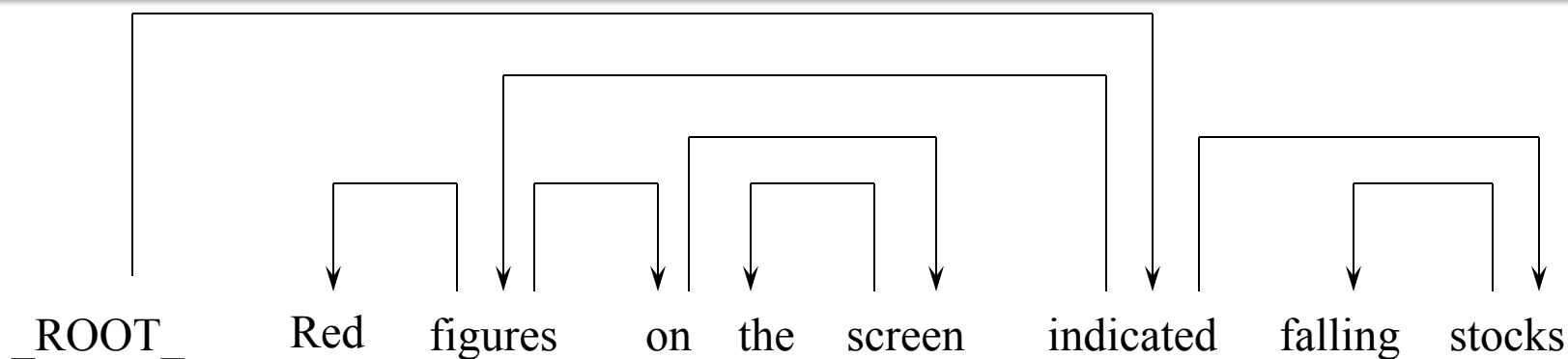


**Combine** spans which overlap in one word; this word must be governed by a word in the left or right span.

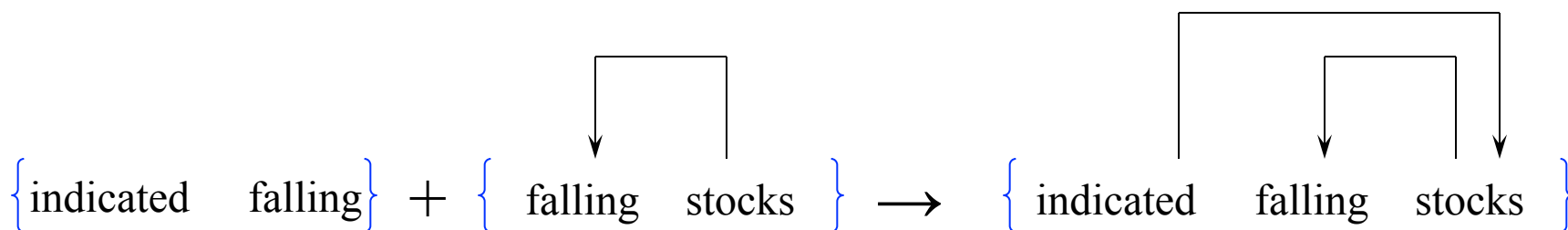
**Invalid span**



# Assembly of correct parse



**Combine** spans which overlap in one word; this word must be governed by a word in the left or right span.





# Features and Unification

# Capturing Grammatical Features

## A Simple Context Free Grammar Fragment

NP  $\rightarrow$  Det N

NP  $\rightarrow$  PropN

Det  $\rightarrow$  a, the, this, those

N  $\rightarrow$  book, dog, books, dogs

PropN  $\rightarrow$  John, Mary

V  $\rightarrow$  sneezed, visited, gave  
eat, eats

S  $\rightarrow$  NP VP

VP  $\rightarrow$  V

(John sneezed)

VP  $\rightarrow$  V NP

(John visited Mary)

VP  $\rightarrow$  V NP NP

(John gave Mary a book)

VP  $\rightarrow$  V NP PP

(John gave a book to Mary)



# Agreement

## Determiner/Noun Agreement

- This dog
- Those dogs

Our grammar also generates

- \*This dogs
- \*Those dog

## Subject/Verb Agreement

- This dog eats
- Those dogs eat

Our grammar also generates

- \*This dog eat
- \*Those dogs eats

# Encoding Number Agreement in CFGs

$NP_{sing} \rightarrow Det_{sing} N_{sing}$

$NP_{pl} \rightarrow Det_{pl} N_{pl}$

$VP_{pl} \rightarrow V_{pl} NP_{sing}$

$VP_{pl} \rightarrow V_{pl} NP_{pl}$

$VP_{sing} \rightarrow V_{sing} NP_{sing}$

$VP_{sing} \rightarrow V_{sing} NP_{pl}$

$S_{sing} \rightarrow NP_{sing} VP_{sing}$

$S_{pl} \rightarrow NP_{pl} VP_{pl}$

**$Det_{sing} \rightarrow$  this**

**$Det_{pl} \rightarrow$  those**

**$N_{sing} \rightarrow$  dog**

**$N_{pl} \rightarrow$  dogs**

**$V_{sing} \rightarrow$  eats**

**$V_{pl} \rightarrow$  eat**

# Subcategorization

- Sneeze: John sneezed
  - \*John sneezed [the book]<sub>NP</sub>
- Find: Please find [a flight to NY]<sub>NP</sub>
  - \*Please find
- Give: Give [me]<sub>NP</sub>[a cheaper fare]<sub>NP</sub>
  - \*Give [with a flight]<sub>PP</sub>
- Prefer: I prefer [to leave earlier]<sub>TO-VP</sub>
  - \*I prefer [United has a flight]<sub>S</sub>

• ...

# Possible CFG Solution

## REPLACE:

- $VP \rightarrow V$
- $VP \rightarrow V NP$
- $VP \rightarrow V NP PP$
- ...

## WITH:

- $VP \rightarrow V_{\text{Intrans}}$
- $VP \rightarrow V_{\text{Trans}} NP$
- $VP \rightarrow V_{\text{Trans+PP}} NP PP$
- $V_{\text{Intrans}} \rightarrow \text{sneeze}$
- $V_{\text{Trans}} \rightarrow \text{find}$
- $V_{\text{Trans+PP}} \rightarrow \text{give}$

# Encoding Number Agreement + Subcats...

- $VP \rightarrow V_{\text{Intrans/sing}}$
- $VP \rightarrow V_{\text{Intrans/pl}}$
- $VP \rightarrow V_{\text{Trans/sing}} \text{ NP}$
- $VP \rightarrow V_{\text{Trans/pl}} \text{ NP}$
- $VP \rightarrow V_{\text{Trans+PP/sing}} \text{ NP PP}$
- $VP \rightarrow V_{\text{Trans+PP/pl}} \text{ NP PP}$
- $V_{\text{Intrans/sing}} \rightarrow \text{sneezes}$
- $V_{\text{Intrans/pl}} \rightarrow \text{sneeze}$
- $V_{\text{Trans/sing}} \rightarrow \text{finds}$
- $V_{\text{Trans/pl}} \rightarrow \text{find}$
- $V_{\text{Trans+PP/sing}} \rightarrow \text{gives}$
- $V_{\text{Trans+PP/pl}} \rightarrow \text{give}$

But what about “I sneeze”, “you sneeze”, “he sneezes”....

# Features, informally

View both words and grammar non-terminals as *complex objects*, each of which has a set of *associated property-value pairs* (called *features*) that can be manipulated.

- Det [num = sg] → this
- Det [num = pl] → those
- N [num = sg] → dog
- N [num = pl] → dogs

Then a grammar can contain:

*NP → Det N but only if Det [num] = N [num]*

# Feature Agreement

OK:

NP  $\rightarrow$  Det N *but only if* Det [num] = N [num]

Better:

NP  $\rightarrow$  Det [num =  $\alpha$ ] N [num =  $\alpha$ ]

Best:

NP [num =  $\alpha$ ]  $\rightarrow$  Det [num =  $\alpha$ ] N [num =  $\alpha$ ]

as well as

S  $\rightarrow$  NP [num =  $\alpha$ ] VP [num =  $\alpha$ ]

# Features and Feature Structures

- We can encode these properties by associating what are called *feature structures* with grammatical constituents.
- A feature structure is a set of *feature-value pairs* where:
  - *features* are atomic symbols
  - *values* are either atomic symbols or (recursively embedded) feature structures

$Feature_1$	$Value_1$
$Feature_2$	$Value_2$
$\vdots$	$\vdots$
$Feature_n$	$Value_n$



# Example Feature Structures

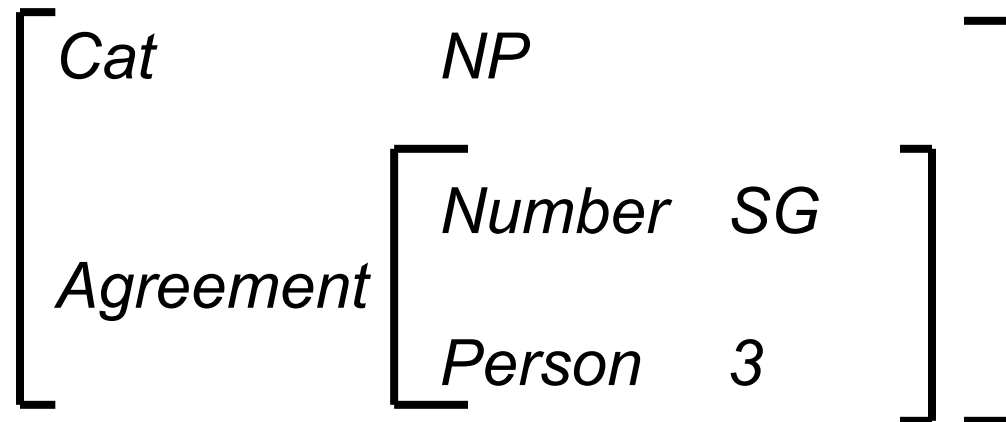
[ *Number*      *SG* ]

[ *Number*      *SG* ]  
[ *Person*      *3* ]

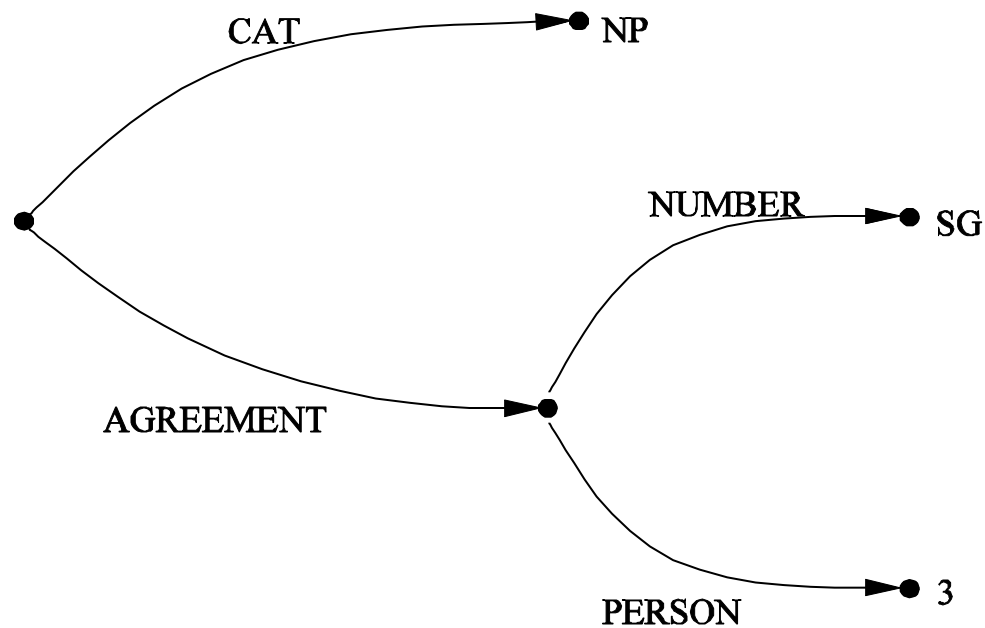
[ *Cat*            *NP* ]  
[ *Number*        *SG* ]  
[ *Person*        *3* ]

# Bundles of Features

- Feature Values can be feature structures themselves.
- This is useful when certain features commonly co-occur, as number and person.

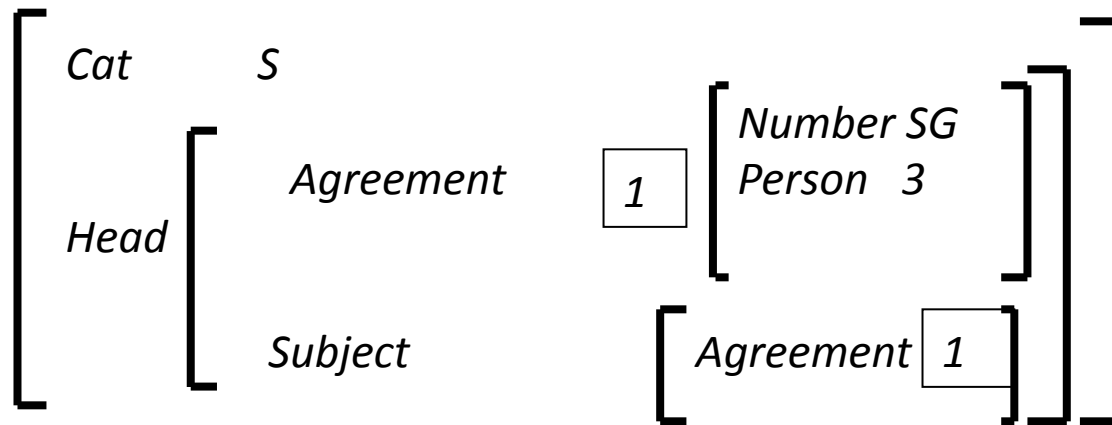


# Feature Structures as DAGs



# Reentrant Structure

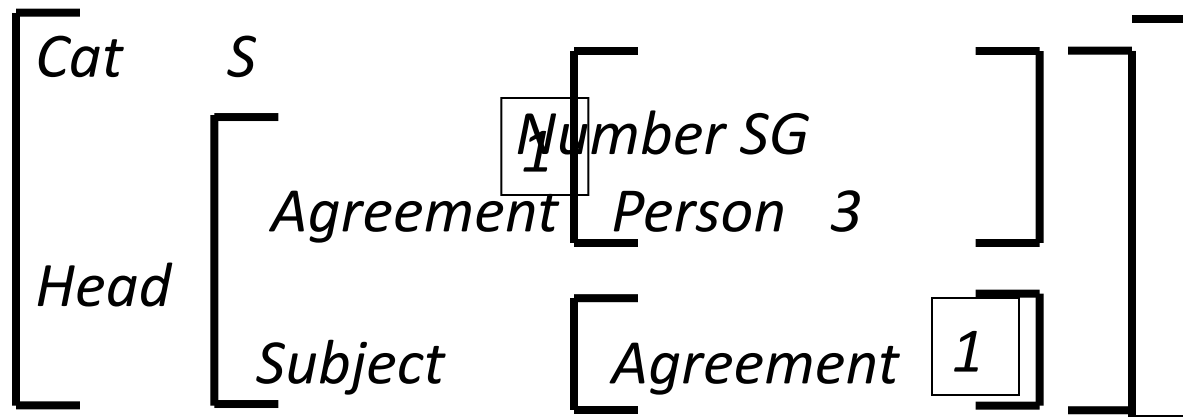
- Multiple features in a feature structure can *share* the same value. In this case they share structure, not just have the same value.



- Numerical indices indicate the shared value.

# Feature Paths

- It will also be useful to talk about paths through feature structures. As in the paths
- <HEAD AGREEMENT NUMBER>
- <HEAD SUBJECT AGREEMENT NUMBER>



# Unification I

## Key operations on feature structures

1. check the compatibility of two structures
2. merge the information in two structures

We can do both with a single operation called *Unification*.

Unifying two feature structures produces a new feature structure that is more specific (has more information) than, or is identical to, each of the input feature structures.

# The Unification Operation: $U$

- Two feature structures can be unified if the component features that make them up are *compatible*.

$[number\ sg] U [number\ sg] = [number\ sg]$   
 $[number\ sg] U [number\ pl] = \text{fails!}$

- Structures are *compatible* if they contain no features that are incompatible.
- If so, unification returns the union of all feature/value pairs.

# The Unification Operation

$$[\textit{Number sg}] \cup [\textit{Number } []] = [\textit{Number sg}]$$

$$[\textit{Number sg}] \cup [\textit{Person 3}] = \left[ \begin{array}{ll} \textit{Number} & \textit{sg} \\ \textit{Person} & 3 \end{array} \right]$$



# The Unification Operation

$\left[ \begin{array}{l} \textit{Agreement}[\textit{Number sg}] \\ \textit{Subject} \quad [\textit{Agreement} \quad [\textit{Number sg}]] \end{array} \right]$

$\cup$

$[\textit{Subject} \quad [\textit{Agreement} \quad [\textit{Person 3}]]]$

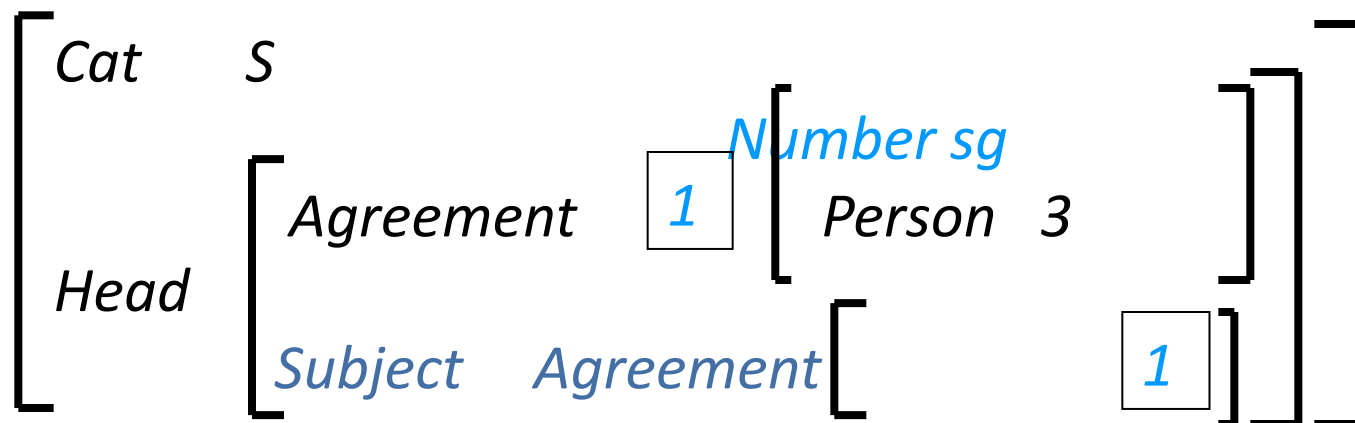
$=$

$\left[ \begin{array}{l} \textit{Agreement}[\textit{Number sg}] \\ \textit{Subject} \quad \left[ \begin{array}{l} \textit{Agreement} \quad \left[ \begin{array}{l} \textit{Number} \quad \textit{sg} \\ \textit{Person} \quad \textit{3} \end{array} \right] \end{array} \right] \end{array} \right]$

# The Unification Operation

*[Head [Subject [Agreement [Number pl] ]]]*

**U**



*= Fail!*

# Properties of Unification

- *Monotonic*: if some description is true of a feature structure, it will still be true after unifying it with another feature structure.
- *Order independent (commutative)*: Unifying a set of feature structures in any order yields the same result.

# Features, Unification, and Grammars

To incorporate all this into grammars:

- Each constituent has a feature-structure associated with it
- Each grammar rule has a (potentially empty) set of *unification constraints* associated with it.
  - The set of unification constraints must be satisfied for the rule to be satisfied.

# Unification Constraints

$X_0 \rightarrow X_1 \dots X_n$  } *Grammar rule*

<  $X_i$  feature path >  
= atomic value

<  $X_i$  feature path >  
= <  $X_k$  feature path >

} *Set of constraints*

# Agreement

NP → Det Nominal

< Det AGREEMENT > = < Nominal AGREEMENT >

< NP AGREEMENT > = < Nominal AGREEMENT >

Noun → flight

< Noun AGREEMENT NUMBER > = SG

Noun → flights

< Noun AGREEMENT NUMBER > = PL

Nominal → Noun

< Nominal AGREEMENT > = < Noun AGREEMENT >

Det → this

< Det AGREEMENT NUMBER > = SG

# Unification and Parsing

- Assume we've augmented our grammar with sets of unification constraints.
- What changes do we need to make to a parser to make use of them?
  1. *Build feature structures* and associate each with a subtree
  2. *Unify feature structures* as subtrees are created from smaller subtrees
  3. *Block ill-formed constituents*

# Unification and Earley Parsing

With respect to an Earley-style parser...

- Build feature structures (represented as DAGs) and associate them with states in the chart
- Unify feature structures as states are advanced in the chart
- Block ill-formed states from entering the chart



# Building Feature Structures

- Features of most grammatical categories are copied from head child to parent
  - (e.g., from V to VP, Nom to NP, N to Nom)

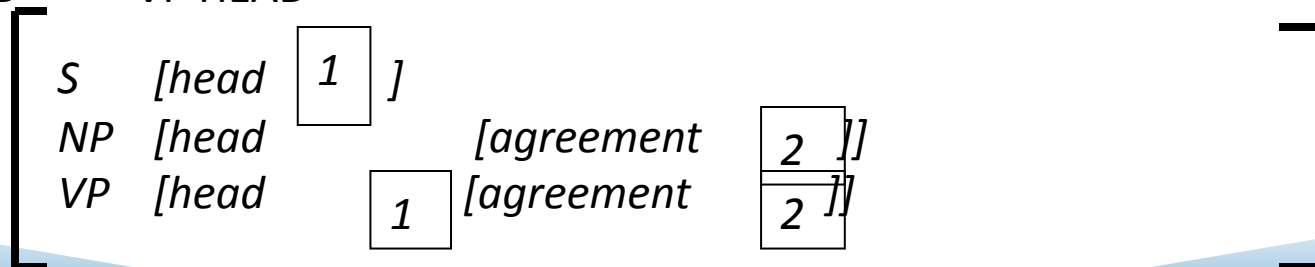
VP → V NP

< VP HEAD > = < V HEAD >

S → NP VP

< NP HEAD AGREEMENT > = < VP HEAD AGREEMENT >

< S HEAD > = < VP HEAD >



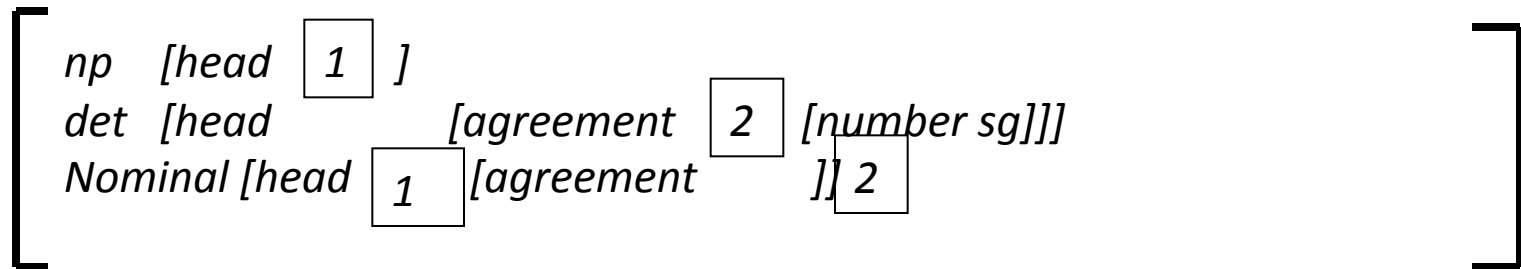
# Augmenting States with DAGs

- We just add a new field to the representation of the states

$S \rightarrow \cdot NP VP, [0,0], \text{Dag}$

# Example

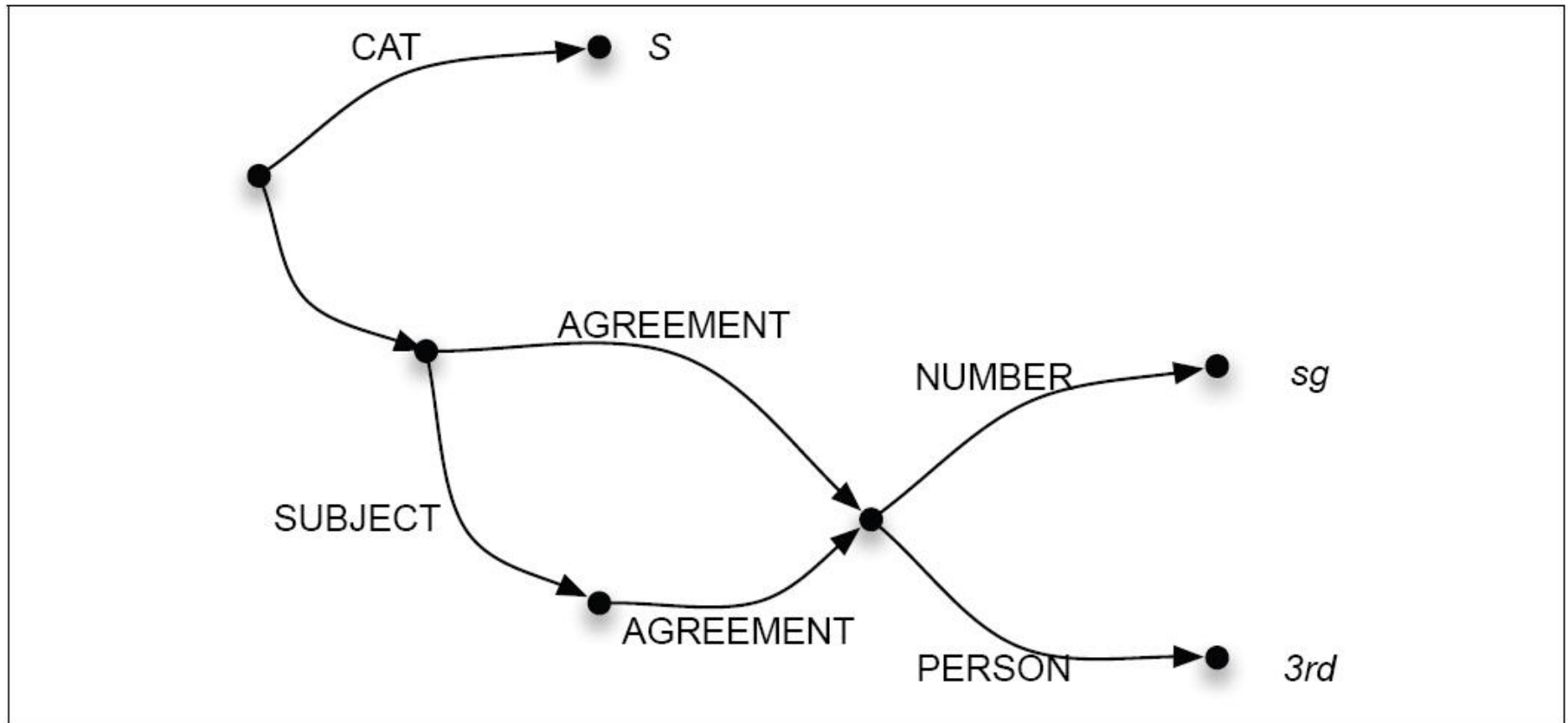
- NP → Det . Nominal [0,1], DAG1



- Nominal → Noun ., [1,2], DAG2



# Figure 15.2



# Unifying States and Blocking

- Keep much of the Earley Algorithm the same.
- We want to unify the DAGs of existing states as they are combined as specified by the grammatical constraints.
- Alter COMPLETER – when a new state is created, first make sure the individual DAGs unify. If so, then add the new DAG (resulting from the unification) to the new state.

# Unification for Semantics

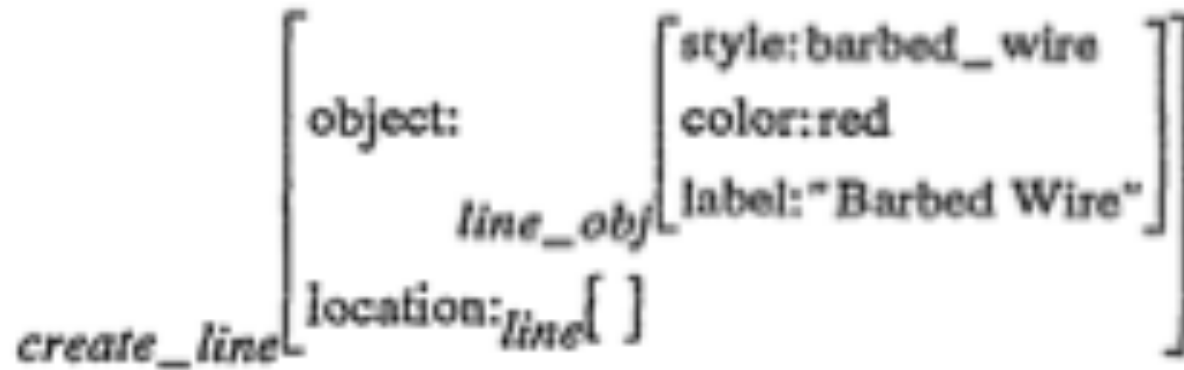


Figure 9: Feature Structure for 'barbed wire'

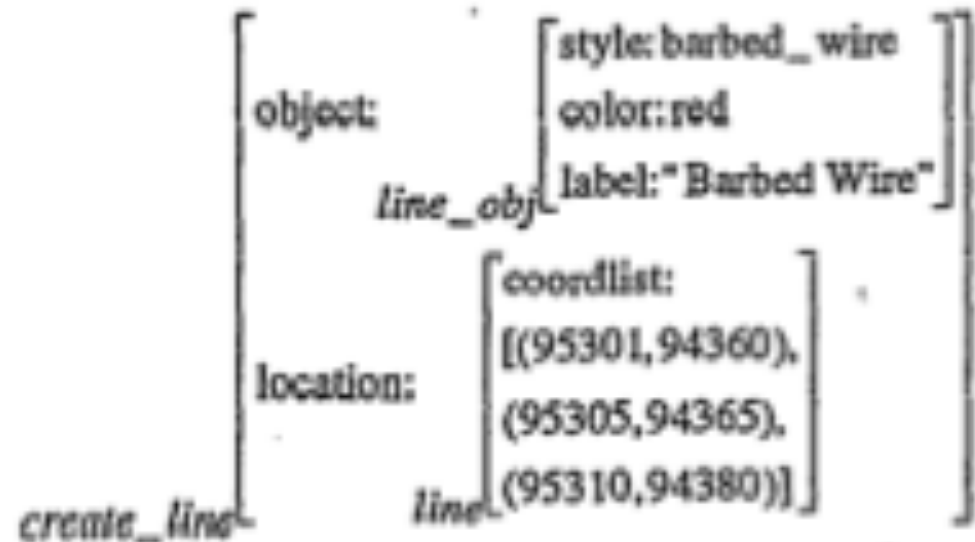


Figure 12: Feature Structure for Multimodal Line Creation