



CS114 Lecture 6

Part of Speech Tagging (POST)

February 3, 2014
Professor Meteer

Thanks for Jurafsky & Martin & Prof. Pustejovsky for slides

Summer JBS

- **Voice, Web and Mobile Applications**
- June 2–August 8, 2014 Professor Timothy Hickey and Professor Marie Meteer
- 3 courses, 12 credits
 - (still checking on status for graduate students)

Next Assignment

- Using a new data set for Switchboard

- text

- {D So } how do you get most of your current event information?

- pos

- / So/UH how/WRB do/VBP [you/PRP] get/VB most/JJS of/IN [your/PRP\$ current/JJ event/NN information/NN] ?/.

- trees

- (SBARQ (INTJ (UH So)) (WHADVP-1 (WRB how)) (SQ (VBP do) (NP-SBJ (PRP you)) (VP (VB get) (NP (NP (JJS most)) (PP (IN of) (NP (PRP\$ your) (JJ current) (NN event) (NN information)))) (ADVP-MNR (-NONE- *T*-1)))) (. ?) (-DFL-E_S))

Goal: Compare sentence parts

- Create corpora of given, new, all
- Separate into test and training
- Run perplexity tools on all the combinations
 - SRILM or CMUCU

	ALL	GIVEN	NEW
ALL			
GIVEN			
NEW			

Part of Speech Tagging

- Parts of speech
 - What's POS tagging good for anyhow?
- Tag sets Rule-based tagging
- Statistical tagging
 - Simple most-frequent-tag baseline
- Important Ideas
 - Training sets and test sets
 - Unknown words
- HMM tagging

Parts of Speech

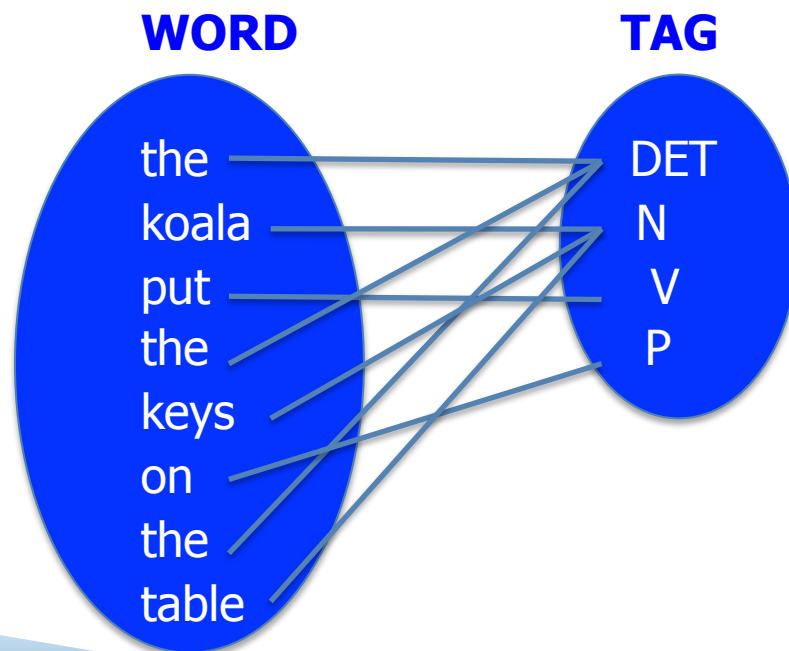
- 8 (ish) traditional parts of speech
 - Noun, verb, adjective, preposition, adverb, article, interjection, pronoun, conjunction, etc
 - Called: parts-of-speech, lexical categories, word classes, morphological classes, lexical tags...
 - Lots of debate within linguistics about the number, nature, and universality of these
 - We'll completely ignore this debate.

POS examples

- N noun *chair, bandwidth, pacing*
- V verb *study, debate, munch*
- ADJ adjective *purple, tall, ridiculous*
- ADV adverb *unfortunately, slowly*
- P preposition *of, by, to*
- PRO pronoun *I, me, mine*
- DET determiner *the, a, that, those*

POS Tagging Definition

- The process of assigning a part-of-speech or lexical class marker to each word in a collection.



Why is POS Tagging Useful?

- First step of a vast number of practical tasks
- Speech synthesis
 - How to pronounce “lead”?
 - INsult inSULT
 - OBject obJECT
 - OVERflow overFLOW
 - DIScount disCOUNT
 - CONtent conTENT
- Parsing
 - Need to know if a word is an N or V before you can parse
- Information extraction
 - Finding names, relations, etc.
- Machine Translation

Open and Closed Classes

- Closed class: a small fixed membership
 - Prepositions: of, in, by, ...
 - Auxiliaries: may, can, will had, been, ...
 - Pronouns: I, you, she, mine, his, them, ...
 - Usually **function words** (short common words which play a role in grammar)
- Open class: new ones can be created all the time
 - English has 4: Nouns, Verbs, Adjectives, Adverbs
 - Many languages have these 4, but not all!

Open Class Words

- **Nouns**
 - Proper nouns (Boulder, Granby, Eli Manning)
 - English capitalizes these.
 - Common nouns (the rest).
 - Count nouns and mass nouns
 - Count: have plurals, get counted: goat/goats, one goat, two goats
 - Mass: don't get counted (snow, salt, communism) (*two snows)
- **Adjectives: tend to modify things**
 - Properties: important
 - Qualities: good, bad
 - Color (blue, gray), age (young, old)

- Verbs
 - Refer to actions or processes
 - Accomplishment vs. process
 - Won vs ran
 - In English, have morphological affixes (eat/eats/eaten)
 - Special closed class of verbs: auxiliaries (be/have)
- Adverbs: tend to modify actions, states, qualities
 - Wide range
 - **Unfortunately**, John walked **home extremely slowly yesterday**
 - Directional/locative adverbs (here, home, downhill)
 - Degree adverbs (extremely, very, somewhat)
 - Manner adverbs (slowly, slinkily, delicately)

Closed Class Words

- prepositions: *on, under, over, ...*
 - Relation between two nouns or verb and noun
- particles: *up, down, on, off, ...*
 - Look like preposition, but change often change the meaning of a verb, e.g. *blow up, turn over*
- determiners: *a, an, the, ...*
- pronouns: *she, who, I, ..*
- conjunctions: *and, but, or, ...*
- auxiliary verbs: *can, may should, ...*
- numerals: *one, two, three, third, ...*

Prepositions from CELEX

of	540,085	through	14,964	worth	1,563	pace	12
in	331,235	after	13,670	toward	1,390	nigh	9
for	142,421	between	13,275	plus	750	re	4
to	125,691	under	9,525	till	686	mid	3
with	124,965	per	6,515	amongst	525	o'er	2
on	109,129	among	5,090	via	351	but	0
at	100,169	within	5,030	amid	222	ere	0
by	77,794	towards	4,700	underneath	164	less	0
from	74,843	above	3,056	versus	113	midst	0
about	38,428	near	2,026	amidst	67	o'	0
than	20,210	off	1,695	sans	20	thru	0
over	18,071	past	1,575	circa	14	vice	0

English Particles

aboard	aside	besides	forward(s)	opposite	through
about	astray	between	home	out	throughout
above	away	beyond	in	outside	together
across	back	by	inside	over	under
ahead	before	close	instead	overhead	underneath
alongside	behind	down	near	past	up
apart	below	east, etc.	off	round	within
around	beneath	eastward(s),etc.	on	since	without

Conjunctions

and	514,946	yet	5,040	considering	174	forasmuch as	0
that	134,773	since	4,843	lest	131	however	0
but	96,889	where	3,952	albeit	104	immediately	0
or	76,563	nor	3,078	providing	96	in as far as	0
as	54,608	once	2,826	whereupon	85	in so far as	0
if	53,917	unless	2,205	seeing	63	inasmuch as	0
when	37,975	why	1,333	directly	26	insomuch as	0
because	23,626	now	1,290	ere	12	insomuch that	0
so	12,933	neither	1,120	notwithstanding	3	like	0
before	10,720	whenever	913	according as	0	neither nor	0
though	10,329	whereas	867	as if	0	now that	0
than	9,511	except	864	as long as	0	only	0
while	8,144	till	686	as though	0	provided that	0
after	7,042	provided	594	both and	0	providing that	0
whether	5,978	whilst	351	but that	0	seeing as	0
for	5,935	suppose	281	but then	0	seeing as how	0
although	5,424	cos	188	but then again	0	seeing that	0
until	5,072	supposing	185	either or	0	without	0

POS Tagging: Choosing a Tagset

- There are so many parts of speech, potential distinctions we can draw
- To do POS tagging, we need to choose a standard set of tags to work with
- Could pick very coarse tagsets
 - N, V, Adj, Adv.
- More commonly used set is finer grained, the “Penn TreeBank tagset”, 45 tags
 - PRP\$, WRB, WP\$, VBG
- Even more fine-grained tagsets exist

Penn TreeBank POS Tagset

Tag	Description	Example	Tag	Description	Example
CC	coordin. conjunction	<i>and, but, or</i>	SYM	symbol	<i>+, %, &</i>
CD	cardinal number	<i>one, two, three</i>	TO	“to”	<i>to</i>
DT	determiner	<i>a, the</i>	UH	interjection	<i>ah, oops</i>
EX	existential ‘there’	<i>there</i>	VB	verb, base form	<i>eat</i>
FW	foreign word	<i>mea culpa</i>	VBD	verb, past tense	<i>ate</i>
IN	preposition/sub-conj	<i>of, in, by</i>	VBG	verb, gerund	<i>eating</i>
JJ	adjective	<i>yellow</i>	VBN	verb, past participle	<i>eaten</i>
JJR	adj., comparative	<i>bigger</i>	VBP	verb, non-3sg pres	<i>eat</i>
JJS	adj., superlative	<i>wildest</i>	VBZ	verb, 3sg pres	<i>eats</i>
LS	list item marker	<i>1, 2, One</i>	WDT	wh-determiner	<i>which, that</i>
MD	modal	<i>can, should</i>	WP	wh-pronoun	<i>what, who</i>
NN	noun, sing. or mass	<i>llama</i>	WP\$	possessive wh-	<i>whose</i>
NNS	noun, plural	<i>llamas</i>	WRB	wh-adverb	<i>how, where</i>
NNP	proper noun, singular	<i>IBM</i>	\$	dollar sign	<i>\$</i>
NNPS	proper noun, plural	<i>Carolinas</i>	#	pound sign	<i>#</i>
PDT	predeterminer	<i>all, both</i>	“	left quote	<i>‘ or “</i>
POS	possessive ending	<i>'s</i>	”	right quote	<i>’ or ”</i>
PRP	personal pronoun	<i>I, you, he</i>	(left parenthesis	<i>[, (, {, <</i>
PRP\$	possessive pronoun	<i>your, one's</i>)	right parenthesis	<i>],), }, ></i>
RB	adverb	<i>quickly, never</i>	,	comma	<i>,</i>
RBR	adverb, comparative	<i>faster</i>	.	sentence-final punc	<i>. ! ?</i>
RBS	adverb, superlative	<i>fastest</i>	:	mid-sentence punc	<i>: ; ... --</i>
RP	particle	<i>up, off</i>			

Using the Penn Tagset

- The/DT grand/JJ jury/NN commmented/VBD on/IN a/DT number/NN of/IN other/JJ topics/NNS ./.
- Prepositions and subordinating conjunctions marked IN (“although/IN I/PRP..”)
- Except the preposition/complementizer “to” is just marked “TO”.

POS Tagging

- Words often have more than one POS: *back*
 - The *back* door = JJ
 - On my *back* = NN
 - Win the voters *back* = RB
 - Promised to *back* the bill = VB
- The POS tagging problem is to determine the POS tag for a particular instance of a word.

How Hard is POS Tagging?

Measuring Ambiguity

	87-tag Original Brown	45-tag Treebank Brown
Unambiguous (1 tag)	44,019	38,857
Ambiguous (2–7 tags)	5,490	8844
Details:		
2 tags	4,967	6,731
3 tags	411	1621
4 tags	91	357
5 tags	17	90
6 tags	2 (<i>well, beat</i>)	32
7 tags	2 (<i>still, down</i>)	6 (<i>well, set, round, open, fit, down</i>)
8 tags		4 (<i>'s, half, back, a</i>)
9 tags		3 (<i>that, more, in</i>)

Three Methods for POS Tagging

1. Rule-based tagging

- (ENGTWOL)

2. Stochastic

1. Probabilistic sequence models

- HMM (Hidden Markov Model) tagging
- MEMMs (Maximum Entropy Markov Models)

3. Transformation Based tagging

- Brill Tagger

Rule-Based Tagging

- Start with a dictionary
- Assign all possible tags to words from the dictionary
- Write rules by hand to selectively remove tags
- Leaving the correct tag for each word.

Start With a Dictionary

- she: PRP
- promised: VBN, VBD
- to TO
- back: VB, JJ, RB, NN
- the: DT
- bill: NN, VB

- Etc... for the ~100,000 words of English with more than 1 tag

Assign Every Possible Tag

PRP	VBN VBD	TO	NN JJ RB VB	DT	VB NN
She	promised	to	back	the	bill

Write Rules to Eliminate Tags

Eliminate VBN if VBD is an option when
VBN|VBD follows “<start> PRP”

PRP	VBN VBD	TO	NN JJ RB VB	DT	VB NN
She	promised	to	back	the	bill

Stage 1 of ENGTWOL Tagging

- First Stage: Run words through FST morphological analyzer to get all parts of speech.
- Example: *Pavlov had shown that salivation ...*

Pavlov	PAVLOV N NOM SG PROPER
had	HAVE V PAST VFIN SVO HAVE PCP2 SVO
shown	SHOW PCP2 SVOO SVO SV
that	ADV PRON DEM SG DET CENTRAL DEM SG
	CS
salivation	N NOM SG

Stage 2 of ENGTWOL Tagging

- Second Stage: Apply NEGATIVE constraints.
- Example: Adverbial “that” rule
 - Eliminates all readings of “that” except the one in
 - “It isn’t that odd”

Given input: “that”

If

(+1 A/ADV/QUANT) ;if next word is adj/adv/quantifier

(+2 SENT-LIM) ;following which is E-O-S

(NOT -1 SVOC/A) ; and the previous word is not a

; verb like “consider” which

; allows adjective complements

; in “I consider that odd”

Then eliminate non-ADV tags

Else eliminate ADV

Statistical Tagging

- Based on probability theory
- First we'll introduce the simple “most-frequent-tag” algorithm
 - Most-freq-tag is another baseline algorithm.
 - Meaning that no one would use it if they really wanted some data tagged
 - But it's useful as a comparison

Conditional Probability and Tags

- $P(\text{Verb})$ is probability of randomly selected word being a verb.
- $P(\text{Verb} | \text{race})$ is “what’s the probability of a word being a verb given that it’s the word “race”?”
 - Race can be a noun or a verb.
 - It’s more likely to be a noun.
- $P(\text{Verb} | \text{race})$ can be estimated by looking at some corpus and saying “out of all the times we saw ‘race’, how many were verbs?”

$$P(V | \text{race}) = \frac{\text{Count}(\text{race is verb})}{\text{Total Count}(\text{race})}$$

Most frequent tag

- Some ambiguous words have a more frequent tag and a less frequent tag:
- Consider the word “a” in these 2 sentences:
 - would/MD prohibit/VB a/DT suit/NN for/IN refund/NN
 - of/IN section/NN 381/CD (/ (a/NN) /) ./.
- Which do you think is more frequent?

Counting in a corpus

- We could count in a corpus
- A corpus: an on-line collection of text, often linguistically annotated
 - The Brown Corpus: 1 million words from 1961 Part of speech tagged at U Penn
 - I counted in this corpus
 - The results for “a”:

21830	DT
6	NN
3	FW

The Most Frequent Tag algorithm

- For each word, we said:
 - Create a dictionary with each possible tag for a word...
- Where does the dictionary come from?
 - One option is to use the same corpus that we use for computing the tags

The/DT City/NNP Purchasing/NNP Department/
NNP ,/, the/DT jury/NN said/VBD,/, is/VBZ
lacking/VBG in/IN experienced/VBN clerical/JJ
personnel/NNS ...



clerical
department
experienced
in
Is
jury
...

Evaluating performance

- How do we know how well a tagger does?
- Say we had a test sentence, or a set of test sentences, that were already tagged by a human
 - a “Gold Standard”
- We could run a tagger on this set of test sentences
- And see how many of the tags we got right.
 - This is called “Tag accuracy” or “Tag percent correct”

Test set

- We take a set of test sentences
 - Hand-label them for part of speech
 - The result is a “Gold Standard” test set
- Who does this?
 - Brown corpus: done by U Penn
 - Grad students in linguistics
- Don’t they disagree?
 - Yes! But on about 97% of tags no disagreements
 - And if you let the taggers discuss the remaining 3%, they often reach agreement
- NOTE: we can’t train our frequencies on the test set sentences.

Computing % correct

- Computing % correct
 - Of all the words in the test set
 - For what percent of them did the tag chosen by the tagger equal the human- selected tag.
- Human tag set: (“Gold Standard” set)

$$\%correct = \frac{\text{\#of words tagged correctly in test set}}{\text{total \# of words in test set}}$$

Unknown Words

- Most-frequent-tag approach has a problem!!
- What about words that don't appear in the training set?
- For example, here are some words that occur in a small Brown Corpus test set but not the training set:

Abernathy	all-american	big-boned
absolution	alligator	boathouses
Adrien	asparagus	boxcar
ajar	baby-sitter	
Alicia	bantered	

Unknown words

- New words added to (newspaper) language 20+ per month
- Plus many proper names ...
- Increases error rates by 1-2%
 - Method 1: assume they are nouns
 - Method 2: assume the unknown words have a probability distribution similar to words only occurring once in the training set.
 - Method 3: Use morphological information, e.g., words ending with -ed tend to be tagged VBN.

Rule-Based Tagger

- **The Linguistic Complaint**
 - Where is the linguistic knowledge of a tagger?
 - Just a massive table of numbers
 - Aren't there any linguistic insights that could emerge from the data?
 - Could thus use handcrafted sets of rules to tag input sentences, for example, if input follows a determiner tag it as a noun.

The Brill tagger

- An example of TRANSFORMATION-BASED LEARNING
- Very popular (freely available, works fairly well)
- A SUPERVISED method: requires a tagged corpus
- Basic idea: do a quick job first (using frequency), then revise it using contextual rules

Brill Tagging: In more detail

- Start with simple (less accurate) rules...learn better ones from tagged corpus
 - Tag each word initially with most likely POS
 - Examine set of **transformations** to see which improves tagging decisions compared to tagged corpus
 - Re-tag corpus using best transformation
 - Repeat until, e.g., performance doesn't improve
 - Result: tagging procedure (ordered list of transformations) which can be applied to new, untagged text

An example

- Examples:
 - They are expected to race tomorrow.
 - The race for outer space.
- Tagging algorithm:
 - Tag all uses of “race” as NN (most likely tag in the Brown corpus)
 - They are expected to race/NN tomorrow
 - the race/NN for outer space
 - Use a transformation rule to replace the tag NN with VB for all uses of “race” preceded by the tag TO:
 - They are expected to race/VB tomorrow
 - the race/NN for outer space

First 20 Transformation Rules

#	Change Tag		Condition
	From	To	
1	NN	VB	Previous tag is <i>TO</i>
2	VBP	VB	One of the previous three tags is <i>MD</i>
3	NN	VB	One of the previous two tags is <i>MD</i>
4	VB	NN	One of the previous two tags is <i>DT</i>
5	VBD	VBN	One of the previous three tags is <i>VBZ</i>
6	VBN	VBD	Previous tag is <i>PRP</i>
7	VBN	VBD	Previous tag is <i>NNP</i>
8	VBD	VBN	Previous tag is <i>VBD</i>
9	VBP	VB	Previous tag is <i>TO</i>
10	POS	VBZ	Previous tag is <i>PRP</i>
11	VB	VBP	Previous tag is <i>NNS</i>
12	VBD	VBN	One of previous three tags is <i>VBP</i>
13	IN	WDT	One of next two tags is <i>VB</i>
14	VBD	VBN	One of previous two tags is <i>VB</i>
15	VB	VBP	Previous tag is <i>PRP</i>
16	IN	WDT	Next tag is <i>VBZ</i>
17	IN	DT	Next tag is <i>NN</i>
18	JJ	NNP	Next tag is <i>NNP</i>
19	IN	WDT	Next tag is <i>VBD</i>
20	JJR	RBR	Next tag is <i>JJ</i>

From: Transformation-Based Error-Driven Learning and Natural Language Processing: A Case Study in Part of Speech Tagging
 Eric Brill. Computational Linguistics. December, 1995.

Transformation Rules for Tagging Unknown Words

Change Tag			
#	From	To	Condition
1	NN	NNS	Has suffix -s
2	NN	CD	Has character .
3	NN	JJ	Has character -
4	NN	VBN	Has suffix -ed
5	NN	VBG	Has suffix -ing
6	??	RB	Has suffix -ly
7	??	JJ	Adding suffix -ly results in a word.
8	NN	CD	The word \$ can appear to the left.
9	NN	JJ	Has suffix -al
10	NN	VB	The word would can appear to the left.
11	NN	CD	Has character 0
12	NN	JJ	The word be can appear to the left.
13	NNS	JJ	Has suffix -us
14	NNS	VBZ	The word it can appear to the left.
15	NN	JJ	Has suffix -ble
16	NN	JJ	Has suffix -ic
17	NN	CD	Has character 1
18	NNS	NN	Has suffix -ss
19	??	JJ	Deleting the prefix un- results in a word
20	NN	JJ	Has suffix -ive

From: Transformation-Based Error-Driven Learning and Natural Language Processing: A Case Study in Part of Speech Tagging
 Eric Brill. Computational Linguistics. December, 1995.

Hidden Markov Model Tagging

- Using an HMM to do POS tagging is a special case of *Bayesian inference*
 - Foundational work in computational linguistics
 - Bledsoe 1959: OCR
 - Mosteller and Wallace 1964: authorship identification
- It is also related to the “noisy channel” model that’s the basis for ASR, OCR and MT

POS Tagging as Sequence Classification

- We are given a sentence (an “observation” or “sequence of observations”)
 - *Secretariat is expected to race tomorrow*
- What is the best sequence of tags that corresponds to this sequence of observations?
- Probabilistic view:
 - Consider all possible sequences of tags
 - Out of this universe of sequences, choose the tag sequence which is most probable given the observation sequence of n words $w_1 \dots w_n$.

Getting to HMMs

- We want, out of all sequences of n tags $t_1 \dots t_n$ the single tag sequence such that $P(t_1 \dots t_n | w_1 \dots w_n)$ is highest.

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$

- Hat ^ means “our estimate of the best one”
- Argmax $f(x)$ means “the x such that $f(x)$ is maximized”

Getting to HMMs

- This equation is guaranteed to give us the best tag sequence

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n)$$

- But how to make it operational? How to compute this value?
- Intuition of Bayesian classification:
 - Use Bayes rule to transform this equation into a set of other probabilities that are easier to compute

Using Bayes Rule

$$P(x|y) = \frac{P(y|x)P(x)}{P(y)}$$

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \frac{P(w_1^n | t_1^n) P(t_1^n)}{P(w_1^n)}$$

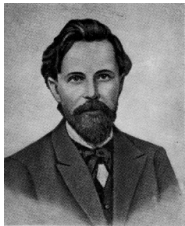
$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(w_1^n | t_1^n) P(t_1^n)$$

Likelihood and Prior



$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} \overbrace{P(w_1^n | t_1^n)}^{\text{likelihood}} \overbrace{P(t_1^n)}^{\text{prior}}$$

$$P(w_1^n | t_1^n) \approx \prod_{i=1}^n P(w_i | t_i)$$



$$P(t_1^n) \approx \prod_{i=1}^n P(t_i | t_{i-1})$$

$$\hat{t}_1^n = \operatorname{argmax}_{t_1^n} P(t_1^n | w_1^n) \approx \operatorname{argmax}_{t_1^n} \prod_{i=1}^n P(w_i | t_i) P(t_i | t_{i-1})$$

Two Kinds of Probabilities

- Tag transition probabilities $p(t_i | t_{i-1})$
 - Determiners likely to precede adjs and nouns
 - That/DT flight/NN
 - The/DT yellow/JJ hat/NN
 - So we expect $P(NN | DT)$ and $P(JJ | DT)$ to be high
 - But $P(DT | JJ)$ to be:
 - Compute $P(NN | DT)$ by counting in a labeled corpus:

$$P(t_i | t_{i-1}) = \frac{C(t_{i-1}, t_i)}{C(t_{i-1})}$$

$$P(NN | DT) = \frac{C(DT, NN)}{C(DT)} = \frac{56,509}{116,454} = .49$$

Two Kinds of Probabilities

- Word likelihood probabilities $p(w_i | t_i)$
 - VBZ (3sg Pres verb) likely to be “is”
 - Compute $P(\text{is} | \text{VBZ})$ by counting in a labeled corpus:

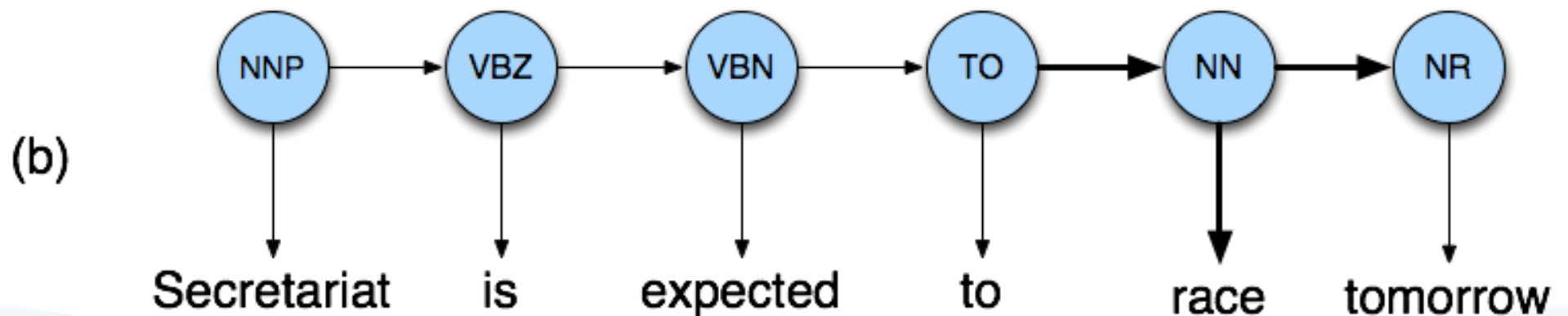
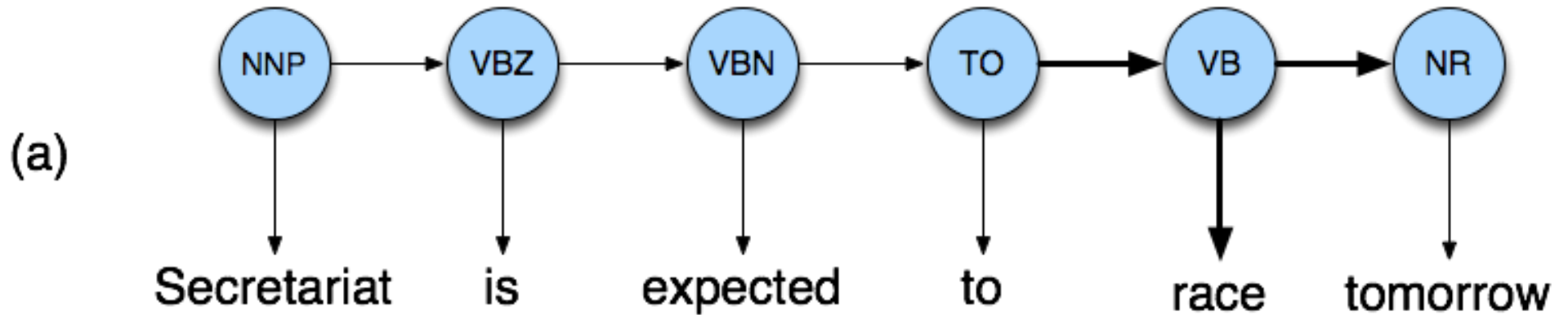
$$P(w_i | t_i) = \frac{C(t_i, w_i)}{C(t_i)}$$

$$P(\text{is} | \text{VBZ}) = \frac{C(\text{VBZ}, \text{is})}{C(\text{VBZ})} = \frac{10,073}{21,627} = .47$$

Example: The Verb “race”

- Secretariat/**NNP** is/**VBZ** expected/**VCN** to/**TO**
race/**VB** tomorrow/**NR**
- People/**NNS** continue/**VB** to/**TO** inquire/**VB** the/**DT**
reason/**NN** for/**IN** the/**DT** **race**/**NN** for/**IN**
outer/**JJ** space/**NN**
- How do we pick the right tag?

Disambiguating “race”



Example

- $P(\text{NN} | \text{TO}) = .00047$
- $P(\text{VB} | \text{TO}) = .83$
- $P(\text{race} | \text{NN}) = .00057$
- $P(\text{race} | \text{VB}) = .00012$
- $P(\text{NR} | \text{VB}) = .0027$
- $P(\text{NR} | \text{NN}) = .0012$
- $P(\text{VB} | \text{TO})P(\text{NR} | \text{VB})P(\text{race} | \text{VB}) = .00000027$
- $P(\text{NN} | \text{TO})P(\text{NR} | \text{NN})P(\text{race} | \text{NN}) = .00000000032$
- So we (correctly) choose the verb reading,

Hidden Markov Models

- What we've described with these two kinds of probabilities is a Hidden Markov Model (HMM)